1.1. 50%. The rightmost page is always the one that is split, leaving two pages that are 50% full. The one on the left stays at 50%.

1.2. Instead of splitting 50/50, split 80/20. The page on the left is 80% full and won't be updated again (within that set of N inserts).

2.1. Candidates:

a: lookup on x = 10, get rows, check y

b: lookup on y between ..., get rows, check x

c: Do both lookups, intersect, get rows.

d: Index checks both conditions, get rows.

e: Index cannot be used.

f: Scan table, check both conditions.

So the possibilities, ranked are: d, c, (a, b), f

2.2. Candidates:

a: -b: -c: Do both lookups, union, get rows. d: -e: -f: Scan table, check both conditions.

Ranked: c, f

2.3 a: (y, x) b: (y, z, x) c: (x, y), (y, z), (z)

```
3.1.
union(X, Y):
   xset = {}
   for each x in X:
      - output x
      - add x to xset
   for each y in Y:
      if y not in xset:
        output y
```

This is faster because we don't have to save and then sort the Y values.

3.2. One pass over X, Y either way, but less memory needed if smaller input is scanned first.

4.1.



4.2. NOT considered:

j3: C and D are not connected by a foreign key or joined in the query.

- j4: Not a left-deep join plan.
- j6: AB and E are not connected by a foreigh key or joined in the query.
- j8: Not a left-deep join plan.
- j9: Not a left-deep join plan.

4.3.

a. Index on Rx

b. seq scan + filter -> index scan
c. T(tid) -> T(tid, z) S(sid) -> S(sid, y)
5.1. T1 < T2 < T3</li>
5.2. T3 < T2 < T1</li>
5.3. T2 < T3 < T1</li>

5.4. T1 Sa should not have been granted. Not serializable:

- a: T1 < T2</li>
- b: T2 < T3</li>
- c: T3 < T1</li>
which is cyclic
6.1: 3 versions:
- a = 1 (initial state)
- a = 2 (T2)
- a = 3 (T3)
6.2: 1
6.3: 1, 1, 1, 1, 1
6.4:
- a: 3

- b: 2 - c: 3 - d: 3 - e: 4

6.5: Block on update. Error (can't serialize) on OTHER commit.